**Problem 4.** Let P be a point inside the triangle ABC. The lines AP, BP and CP intersect the circumcircle  $\Gamma$  of triangle ABC again at the points K, L and M respectively. The tangent to  $\Gamma$  at C intersects the line AB at S. Suppose that SC = SP. Prove that MK = ML.

**Problem 5.** In each of six boxes  $B_1, B_2, B_3, B_4, B_5, B_6$  there is initially one coin. There are two types of operation allowed:

- Type 1: Choose a nonempty box  $B_j$  with  $1 \le j \le 5$ . Remove one coin from  $B_j$  and add two coins to  $B_{j+1}$ .
- Type 2: Choose a nonempty box  $B_k$  with  $1 \le k \le 4$ . Remove one coin from  $B_k$  and exchange the contents of (possibly empty) boxes  $B_{k+1}$  and  $B_{k+2}$ .

Determine whether there is a finite sequence of such operations that results in boxes  $B_1, B_2, B_3, B_4, B_5$  being empty and box  $B_6$  containing exactly  $2010^{2010^{2010}}$  coins. (Note that  $a^{b^c} = a^{(b^c)}$ .)

**Problem 6.** Let  $a_1, a_2, a_3, \ldots$  be a sequence of positive real numbers. Suppose that for some positive integer s, we have

$$a_n = \max\{a_k + a_{n-k} \mid 1 \le k \le n - 1\}$$

for all n > s. Prove that there exist positive integers  $\ell$  and N, with  $\ell \leq s$  and such that  $a_n = a_\ell + a_{n-\ell}$  for all  $n \geq N$ .